

91577



NEW ZEALAND QUALIFICATIONS AUTHORITY
MANA TOHU MĀTAURANGA O AOTEAROA

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SUPERVISOR'S USE ONLY

Level 3 Calculus, 2016

91577 Apply the algebra of complex numbers in solving problems

9.30 a.m. Wednesday 23 November 2016
Credits: Five

Achievement	Achievement with Merit	Achievement with Excellence
Apply the algebra of complex numbers in solving problems.	Apply the algebra of complex numbers, using relational thinking, in solving problems.	Apply the algebra of complex numbers, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

You should attempt ALL the questions in this booklet.

Show ALL working.

Make sure that you have the Formulae and Tables Booklet L3–CALCF.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

Check that this booklet has pages 2–8 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.

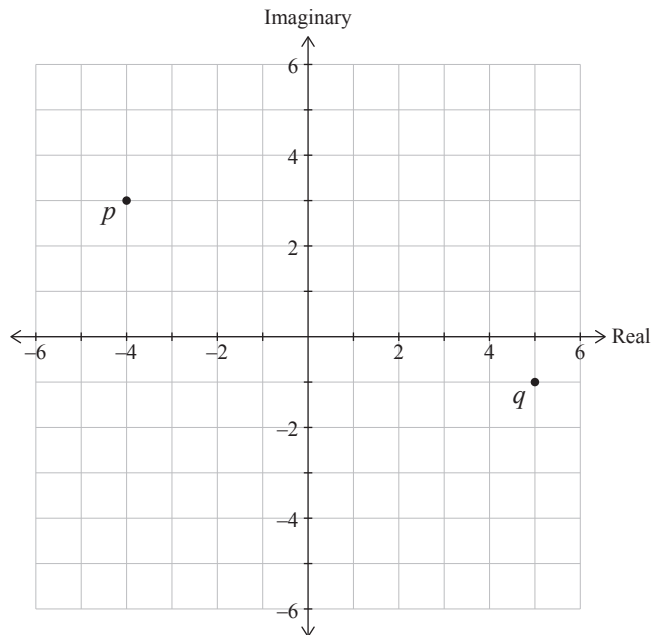
TOTAL

ASSESSOR'S USE ONLY

QUESTION ONE

- (a) Complex numbers p and q are represented on the Argand diagram.

If $s = p + q$, then show s on the Argand diagram below.



- (b) Dividing $2x^3 + 5x^2 + Ax + 7$ by $x + 3$ gives a remainder of 16.

What is the value of A?

- (c) Solve the equation $5 - \sqrt{x} = \sqrt{x - p}$ for x in terms of p .

- (d) If $w = 1 + 2i$, find the value of $w^2 + \frac{w}{w}$, giving your answer in the form $a + bi$, where a and b are real.

You must clearly show each step of your working.

- (e) The locus described by $|z - 2 + 3i| = |z - 1|$ is a straight line.

Find the gradient of that line.

QUESTION TWO

- (a) Solve the equation $x^2 - 6x + 12 = 0$.

Write your answer in the form $a \pm \sqrt{b}i$, where a and b are rational numbers.

- (b) $u = 2 + 3i$ and $v = 5 + mi$.

Find the value of m if $uv = 22 + 7i$.

- (c) Solve the equation $z^3 = -8k^6$, where k is real.

Write your solutions in polar form in terms of k .
