

**Assessment Schedule – 2021****Mathematics and Statistics: Apply geometric reasoning in solving problems (91031)****Evidence**

Do not penalise incorrect rounding if sufficient evidence provided.

<b>Q ONE</b>	<b>Evidence</b>	<b>Achievement</b>	<b>Achievement with Merit</b>	<b>Achievement with Excellence</b>
(a) (i)	Use of Trigonometry to find $PL = 18 \times \tan 20$ $= 18 \times 0.36397$ $x = 6.55 \text{ cm}$	Showing, with evidence of working, that $PL = x = 6.55 \text{ cm}$ . <i>2dp confirms the correct working.</i>		
(ii)	Use of Trigonometry to find $y = \cos^{-1}\left(\frac{18}{35}\right)$ $= \cos^{-1}(0.5143)$ $y = 59.1^\circ$	Showing, with evidence of working, that $y = 59.1^\circ$		
(b) (i)	In triangle AEF, $x^2 + x^2 = 2^2$ (Pythagoras) $2x^2 = 4$ $x^2 = 2$ $x = 1.4142$ OR $\sin 45^\circ = \frac{AF}{2}$ (trigonometry) $AF = 2 \times \sin 45^\circ$ $AF = 2 \times 0.7071$ $AF = 1.4142 \text{ cm}$ OR OR alternatively use $\cos 45^\circ$ .	Forms a correct Pythagoras equation.  OR Forms a correct trigonometry equation.	Correct value for AF (or equivalent) $AF = 1.4142$ , with clear evidence of working.	
(ii)	Then $BF = 20 - 1.4142 = 18.5858$  In triangle FBG, $w^2 = 18.5858^2 + 18.5858^2$ $w^2 = 690.86$ $w = 26.28 \text{ cm}$ OR $\sin 45^\circ = \frac{20 - 1.4142}{w}$ $w = \frac{18.5858}{\sin 45^\circ} = 26.284$ OR alternatively use $\cos 45^\circ$ .	Correct length $w = 26.28 \text{ cm}$ found, with evidence of working.		

(c)	<p>In triangle BCF,  <math>FC = 6 \times \tan 52^\circ</math>  <math>= 6 \times 1.2799</math>  <math>FC = 7.68 \text{ cm.}</math></p> <p><math>AB = 30 - 7.68 = 22.32 \text{ cm.}</math></p> <p>In triangle ABE,          Use of Trigonometry to find  <math display="block">p = \cos^{-1}\left(\frac{22.32}{33}\right)</math>  <math>= \cos^{-1}(0.6764)</math>  <math>p = 47.4^\circ</math></p> <p>OR alternative method.</p>	<p>Showing, with evidence of working, that  <math>FC = 7.68 \text{ cm.}</math></p> <p>OR</p> <p>Evaluation of angle <math>p</math>, with consistency,          with evidence of working.</p>	<p>Correct value          of <math>p = 47.4^\circ</math> found,          with clear evidence          of working.</p>	
(d)	<p>Use of Pythagoras in triangle ABH,  <math>AB = \sqrt{17^2 - 2^2}</math>  <math>AB = \sqrt{285}</math>  <math>AB = 16.88 \text{ cm}</math>  <math>CG = 16.88 - 4 = 12.88 \text{ cm.}</math></p> <p>Use of trigonometry in triangle ADG,  <math>AD = 4 \times \tan 65^\circ</math>  <math>= 4 \times 2.1445</math>  <math>AD = 8.58 \text{ cm.}</math>  <math>CH = 8.58 - 2 = 6.58 \text{ cm.}</math></p> <p>Use of trigonometry in triangle ADG,  <math display="block">AG = \frac{4}{\cos 65^\circ}</math>  <math>AG = 9.46 \text{ cm.}</math></p> <p>Use of Pythagoras in triangle CGH,  <math>GH = \sqrt{12.88^2 + 6.58^2}</math>  <math>GH = \sqrt{209.19}</math>  <math>GH = 14.46 \text{ cm}</math>  <math>\text{Total Distance} = 9.46 + 14.46 + 17</math>  <math>= 40.92 \text{ cm.}</math></p> <p>OR alternative method.</p>	<p>Finding, with evidence          of working, any ONE of:</p> <ul style="list-style-type: none"> <li>• Length AB = 16.88</li> <li>• Length AD = 8.58 cm</li> <li>• Length AG = 9.46 cm</li> <li>• Length GH = 14.46 cm.</li> </ul> <p><i>2dp required (or clear method shown) to exclude incorrect assumption of the red triangle as being right-angled.</i></p>	<p>Finding, with          evidence of working,          any TWO of:</p> <ul style="list-style-type: none"> <li>• Length GC = 12.88</li> <li>• Length CH = 6.58</li> <li>• Length AG = 9.46</li> <li>• Length GH = 14.46</li> </ul>	<p><b>T2 / E8</b>          Finding, with          evidence of          working, the total          length 40.92 cm.</p> <p><b>T1 / E7</b>          Identifies, with          evidence of          working, the          lengths of the two          remaining sides of          the red triangle:  <math>AG = 9.46</math>          and <math>GH = 14.46</math>          OR          Identifies, with          evidence of          working, a          consistent total          length, with an          earlier minor error  <i>A minor error          could be for          example: an          arithmetic error          or omitting only          one of the          subtractions of          2cm or 4 cm but          not both of them.</i></p>

N0	N1	N2	A3	A4	M5	M6	E7	E8
No response; no relevant evidence.	One point made incompletely.	1 of u	2 of u	3 of u	1 of r	2 of r	T1	T2

Q TWO	Evidence	Achievement	Achievement with Merit	Achievement with Excellence
(a) (i)	$\angle HPE = 77^\circ$ (vertically opposite angles are equal). $\angle FHE = 81^\circ$ (angles in the same segment / sector are equal) $x = \angle HEG = 180 - 77 - 81 = 22^\circ$ (angles in a triangle add to $180^\circ$ )  OR $\angle GFP = 180 - 81 - 77 = 22^\circ$ (angles in a triangle add to $180^\circ$ ) $x = \angle HEG = 22^\circ$ (angles in the same segment / sector are equal)  OR alternative method.	Required angle $x = 22^\circ$ found, with some evidence, which could be on the diagram.  (Reasons not necessary)		
(a) (ii)	$\angle FCE = 2 \times 81 = 162^\circ$ (angle at the centre is twice that at the circumference) $\angle ECF = 360 - 162^\circ = 198^\circ$ (angles at a point sum to $360^\circ$ )  OR alternative method.	Required angle $y = 198^\circ$ found.  (Reasons not necessary.)		
(b)	$\angle PQC = 90^\circ$ (angle between tangent and radius is a right-angle) In triangle PQW, $\angle PWQ = 180 - 90 - 40 = 50^\circ$ (angle sum of triangle PQW is $180^\circ$ ) $\angle CVW = 50^\circ$ (base angles of an isosceles triangle are equal) $\angle VCW = 180 - 50 - 50 = 80^\circ$ (angle sum of triangle CVW is $180^\circ$ ) $\angle QCV = e = 180 - 80 = 100^\circ$ (adjacent angles on a straight line)  OR alternative method.	Finding two angles from: <ul style="list-style-type: none"> <li><math>\angle PQC = 90^\circ</math></li> <li><math>\angle PWQ = 50^\circ</math></li> <li><math>\angle CVW = 50^\circ</math></li> <li><math>\angle VCW = 80^\circ</math></li> </ul> OR One of these angles with a valid reason.  OR CAO.  <i>Angles could be shown on the diagram.</i>	Required angle $e = 100^\circ$ found, with at least one valid reason.	

(c)	$\angle KQN = 180 - 90 - 38 = 52^\circ$ (angle sum of triangle NKQ) $\angle KQM = 180 - 52 = 128^\circ$ (adjacent angles on a straight line) $\angle QLM = \frac{(180 - 128)}{2} = 26^\circ$ (base angles of isosceles triangle are equal) $y = \angle KLM = 180 - 26 = 154^\circ$ (adjacent angles on straight line)  OR alternative method.	Finding two angles from $\angle KQN = 52^\circ$ or $\angle KQM = 128^\circ$ or $\angle QLM = 26^\circ$  OR One of these angles with a valid reason (consistency applies).  OR CAO.	Required angle $y = 154^\circ$ found, with at least one valid reason.	
(d)	$\angle PRW = 90^\circ$ (angle in a semicircle is a right angle)  $\angle PWR = 180 - y^\circ$ (adjacent angles on a straight line)  $\angle PQR = 180 - (180 - y) = y$ (opposite angles of a cyclic quad add up to 180)  $\angle QRP = 180 - x - y$ (angle sum of triangle PQR)  $\angle SRW = 180 - 90 - (180 - x - y)$ $= x + y - 90$ (adjacent angles on a straight line)  $\angle RSW = 180 - y - (x + y - 90)$ $\angle z = 180 - y - x - y + 90^\circ$ $\angle z = 270^\circ - x - 2y$ OR alternative method.	One step shown involving calculation of an angle involving $x$ or $y$  i.e. Finding $\angle PWR = 180 - y$ or $\angle PQR = y$ or $\angle QRP = 180 - x - y$ or $\angle SRW = 180 - z - y$  OR two steps, having substituted numerical values for $x$ and $y$ .  OR  CAO	Finding TWO angles involving calculations including $x$ or $y$ , with at least one valid reason.  OR  Finding the value of $z$ , having substituted numerical values for $x$ and $y$ .	<b>T2 / E8</b> Finding $\angle z$ , in terms of $x$ and $y$ , with clear justification. $z = 270 - x - 2y$  <b>T1 / E7</b> Finding $\angle z$ , in terms of $x$ and $y$ , with unclear justification or not simplified. OR Minor error, e.g. incorrect algebraic rearrangement.

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No response; no relevant evidence.	One point made incompletely.	1 of u	2 of u	3 of u	1 of r	2 of r	T1	T2

Q THREE	Evidence	Achievement	Achievement with Merit	Achievement with Excellence
(a)	<p>Use of trigonometry to find</p> $\angle XWY = \sin^{-1} \frac{33}{85}$ $= 22.84^\circ$ <p>Then <math>\angle f = 90 - 22.84 = 67.16^\circ</math></p> <p>OR</p> <p>Use of trigonometry to find</p> $\angle WYX = \cos^{-1} \frac{33}{85}$ $= 67.16^\circ$ <p>Then <math>\angle f = 67.16^\circ</math></p> <p>(alternate angles between parallel lines are equal)</p> <p>OR alternative method.</p>	<p>Showing, with evidence of working, that <math>f = 67.16^\circ</math>.</p>		
(b)	<p>Similar triangles recognised and <math>g</math> calculated using ratio of sides:</p> $\frac{g + 4.64}{10.26} = \frac{4.64}{2.85}$ $g = 12.064 \text{ cm}$ <p>OR ratio of 3.6 (or its reciprocal, 0.272) calculated and correctly used:</p> $\frac{RS}{QT} = \frac{10.26}{2.85} = 3.6$ <p>Then <math>\frac{PS}{PT} = 3.6</math></p> $PS = 3.6 \times 4.64$ $PS = 16.704$ <p>Then <math>g = 16.704 - 4.64</math></p> $g = 12.064 \text{ cm.}$ <p>Justification of similar triangles not required.</p> <p>OR</p> <p>Use of trigonometry to find</p> $\angle QPT = \tan^{-1} \frac{2.85}{4.64} = 31.56^\circ$ <p>Then in triangle RPS,</p> $\tan 31.56 = \frac{10.26}{PS}$ $PS = \frac{10.26}{\tan 31.56}$ $PS = \frac{10.26}{0.6142}$ $PS = 16.704$ <p>Then <math>g = 16.704 - 4.64</math></p> $g = 12.064 \text{ cm.}$ <p>OR alternative method.</p>	<p>Forming an equation involving a correct ratio of similar sides.</p> <p>OR</p> <p>Finding a correct ratio involving similar triangles</p> <p>e.g. of 3.6</p> <p>or its reciprocal 0.2727 with evidence.</p> <p>OR</p> <p>Finding angle of <math>\angle QPT = 31.56^\circ</math> with evidence.</p> <p>OR</p> <p>CAO.</p>	<p>Calculation of correct value of <math>g = 12.064 \text{ cm}</math> with evidence of working.</p>	

(c)(i)	Use of bearings and geometry to find $\angle ABG = 180 - 128 = 52^\circ$ (co-interior angles between parallel lines add to $180^\circ$ ) (or equivalent) CAO is not sufficient.	Showing, with evidence of working, that $\angle ABG = u = 52^\circ$  Reasons not necessary.		
(c)(ii)	$\angle CBH = 180 - 90 - 52 = 38^\circ$ (adjacent angles on a straight line) $\angle KCB = 38^\circ$ (alternate angles between parallel lines are equal) $\angle BCH = 90 - 38 = 52^\circ$  Use of trigonometry in triangle ABC, $\angle ACB = \tan^{-1}\left(\frac{1500}{800}\right)$ $\angle ACB = 61.93^\circ$ $\angle ACJ = 180 - 61.93^\circ - 52 = 66.07^\circ$ Required bearing = $270^\circ + 66.07^\circ = 336.07^\circ$ OR alternative method.	Finding, with evidence of working, that $\angle ACB = 61.93^\circ$  OR One relevant length, with evidence of working: $BG = 923.49 \text{ km}$ $BH = 630.41 \text{ km}$ $AG = 1700 \text{ km}$  OR CAO	Correct bearing of $336.7^\circ$ .	
(d)(i)	Using trigonometry / Pythagoras in triangle ABC, $AB = 86 \times \cos 56^\circ$ $AB = 48.09 \text{ metres}$  Using trigonometry / Pythagoras in triangle ABC, $BC = 86 \times \sin 56^\circ$ $BC = 71.30 \text{ metres}$  Using trigonometry in triangle ABT, $\text{Height} = BT = 48.09 \times \tan 32^\circ$ $\text{Tower Height} = 30.05 \text{ metres}$ .	One correct length, with evidence of working from: <ul style="list-style-type: none"> <li><math>AB = 48.09</math></li> <li><math>BC = 71.30</math></li> </ul> OR  CAO	Proving tower height of $30.05 \text{ m}$ .  OR Consistent angle of elevation.  OR Both lengths AB and BC found, with evidence.	E8 Clear evidence Proving tower height of $30.05 \text{ m}$ . AND Correct angle of elevation of $22.85^\circ$ , with evidence.  E7 Clear evidence Proving tower height of $30.05 \text{ m}$ AND Finds a consistent angle of elevation with a minor error in working.
(ii)	Using trigonometry in triangle BCT, $\angle BCT = \tan^{-1}\left(\frac{30.05}{71.30}\right)$ $\angle BCT = \tan^{-1}(0.4215)$ Required angle of elevation is $\angle BCT = 22.85^\circ$ OR alternative method.			

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No response; no relevant evidence.	One point made incompletely.	1 of u	2 of u	3 of u	1 of r	2 of r	Q 2 (d) with minor error.	Q 2 (d)

**Cut Scores**

<b>Not Achieved</b>	<b>Achievement</b>	<b>Achievement with Merit</b>	<b>Achievement with Excellence</b>
0 – 6	7 – 14	15 – 20	21 – 24