



deg	rad
30°	$\frac{\pi}{6}$
90°	$\pi/2$
45°	$\frac{\pi}{4}$
60°	$\frac{\pi}{3}$

$$\sin \theta = \frac{O}{H}$$

$$\sin 30 = \frac{1}{2}$$

$$\sin 45 = \frac{1}{\sqrt{2}}$$

$$\sin 60 = \frac{\sqrt{3}}{2}$$

$$\cos \theta = \frac{A}{H}$$

$$\cos 30 = \frac{\sqrt{3}}{2}$$

$$\cos 45 = \frac{1}{\sqrt{2}}$$

$$\cos 60 = \frac{1}{2}$$

$$\tan \theta = \frac{O}{A}$$

$$\tan 30 = \frac{1}{\sqrt{3}}$$

$$\tan 45 = 1$$

$$\tan 60 = \sqrt{3}$$

$$\operatorname{cosec} \theta = \frac{H}{O}$$

$$\operatorname{cosec} 30 = \frac{2}{1} = 2$$

$$\operatorname{cosec} 45 = \frac{\sqrt{2}}{1} = \sqrt{2}$$

$$\operatorname{cosec} 60 = \frac{2}{\sqrt{3}}$$

$$\sec \theta = \frac{H}{A}$$

$$\sec 30 = \frac{2}{\sqrt{3}}$$

$$\sec 45 = \frac{\sqrt{2}}{1} = \sqrt{2}$$

$$\sec 60 = \frac{2}{1} = 2$$

$$\cot \theta = \frac{A}{O}$$

$$\cot 30 = \frac{\sqrt{3}}{1} = \sqrt{3}$$

$$\cot 45 = 1$$

$$\cot 60 = \frac{1}{\sqrt{3}}$$

$$\sin 75 = \sin(45 + 30) = \sin 45 \cos 30 + \cos 45 \sin 30 = \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{2} = \frac{\sqrt{3}}{2\sqrt{2}} + \frac{1}{2\sqrt{2}} = \frac{\sqrt{3} + 1}{2\sqrt{2}}$$

$$\sin 105 = \sin(45 + 60) = \sin 45 \cos 60 + \cos 45 \sin 60 = \frac{1}{\sqrt{2}} \times \frac{1}{2} + \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} = \frac{1}{2\sqrt{2}} + \frac{\sqrt{3}}{2\sqrt{2}} = \frac{1 + \sqrt{3}}{2\sqrt{2}}$$

$$\sin 90 = \sin(30 + 60) = \sin 30 \cos 60 + \cos 30 \sin 60 = \frac{1}{2} \times \frac{1}{2} + \frac{\sqrt{3}}{2} \times \frac{\sqrt{3}}{2} = \frac{1}{4} + \frac{3}{4} = 1$$

$$\cos 75 = \cos(45 + 30) = \cos 45 \cos 30 - \sin 45 \sin 30 = \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} - \frac{1}{\sqrt{2}} \times \frac{1}{2} = \frac{\sqrt{3}}{2\sqrt{2}} - \frac{1}{2\sqrt{2}} = \frac{\sqrt{3} - 1}{2\sqrt{2}}$$

$$\cos 105 = \cos(45 + 60) = \cos 45 \cos 60 - \sin 45 \sin 60 = \frac{1}{\sqrt{2}} \times \frac{1}{2} - \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} = \frac{1}{2\sqrt{2}} - \frac{\sqrt{3}}{2\sqrt{2}} = \frac{1 - \sqrt{3}}{2\sqrt{2}}$$

$$\cos 90 = \cos(30 + 60) = \cos 30 \cos 60 - \sin 30 \sin 60 = \frac{\sqrt{3}}{2} \times \frac{1}{2} - \frac{1}{2} \times \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{4} - \frac{\sqrt{3}}{4} = 0$$

$$\tan 75 = \tan(45 + 30) = \frac{\tan 45 + \tan 30}{1 - \tan 45 \tan 30} = \frac{1 + \frac{1}{\sqrt{3}}}{1 - \frac{1}{\sqrt{3}}}$$

$$\tan 105 = \tan(45 + 60) = \frac{\tan 45 + \tan 60}{1 - \tan 45 \tan 60} = \frac{1 + \sqrt{3}}{1 - \sqrt{3}}$$

$$\tan 90 = \tan(30 + 60) = \frac{\tan 30 + \tan 60}{1 - \tan 30 \tan 60} = \frac{\frac{1}{\sqrt{3}} + \sqrt{3}}{1 - 1} = \frac{\sqrt{3} + \frac{1}{\sqrt{3}}}{0} = \text{unidentified}$$

$$\sin 15 = \sin(45 - 30) = \sin 45 \cos 30 - \cos 45 \sin 30 = \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} - \frac{1}{\sqrt{2}} \times \frac{1}{2} = \frac{\sqrt{3}}{2\sqrt{2}} - \frac{1}{2\sqrt{2}} = \frac{\sqrt{3}-1}{2\sqrt{2}}$$

$$\cos 15 = \cos(45 - 30) = \cos 45 \cos 30 + \sin 45 \sin 30 = \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{2} = \frac{\sqrt{3}}{2\sqrt{2}} + \frac{1}{2\sqrt{2}} = \frac{\sqrt{3}+1}{2\sqrt{2}}$$

$$\tan 15 = \tan(45 - 30) = \frac{\tan 45 - \tan 30}{1 + \tan 45 \tan 30} = \frac{1 - \frac{1}{\sqrt{3}}}{1 + \frac{1}{\sqrt{3}}}$$

$$\operatorname{cosec} 75 = \frac{2\sqrt{2}}{\sqrt{3}+1} \quad \sec 75 = \frac{2\sqrt{2}}{\sqrt{3}-1} \quad \cot 75 = \frac{1 + \frac{1}{\sqrt{3}}}{1 - \frac{1}{\sqrt{3}}}$$

$$\operatorname{cosec} 105 = \frac{2\sqrt{2}}{1+\sqrt{3}} \quad \sec 105 = \frac{2\sqrt{2}}{1-\sqrt{3}} \quad \cot 105 = \frac{1-\sqrt{3}}{1+\sqrt{3}}$$

$$\operatorname{cosec} 90 = 1 \quad \sec 90 = 0 \quad \cot 90 = \text{unidentified}$$

$$\operatorname{cosec} 15 = \frac{2\sqrt{2}}{\sqrt{3}-1} \quad \sec 15 = \frac{2\sqrt{2}}{1+\sqrt{3}} \quad \cot 15 = \frac{1 + \frac{1}{\sqrt{3}}}{1 - \frac{1}{\sqrt{3}}}$$