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SUPERVISOR'S USE ONLY

91261



Level 2 Mathematics and Statistics, 2015 91261 Apply algebraic methods in solving problems

2.00 p.m. Tuesday 10 November 2015 Credits: Four

Achievement	Achievement with Merit	Achievement with Excellence
Apply algebraic methods in solving problems.	Apply algebraic methods, using relational thinking, in solving problems.	Apply algebraic methods, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

You should attempt ALL the questions in this booklet.

Make sure that you have Resource Sheet L2-MATHF.

Show ALL working.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

You are required to show algebraic working in this paper. Guess-and-check methods and correct answer(s) only will generally limit grades to Achievement.

Check that this booklet has pages 2–11 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.

Not Achieved

7

Annotated Exemplar Template

Not	Achieved ex	xemplar for 91261 2015 Total score 07			
Q	Grade score	Annotation			
1	А3	While the answer to 1aii was correct it did not provide evidence as the rearrangement of the log equation was incorrect, the candidate had only taken logs of one side in 1b and neither parts of 1c provided evidence.			
2	N2	Only 2a provided evidence, gaining u for a consistent simplification following incorrect factorisation.		llowing	
3	N2	Question 3aii provided partial evidence (u) with x³ a cattempts were either incomplete or incorrect.	correct term, all o	ther	

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(.)	IFST	IC JIN	ON	ь.

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(a) (i) Find the value of $\log_2 1024$.

 $\log_2 1024 = \log_2 2^{2} = \log_2 1024$

10g 1024 = x log 2. 2= 10

(ii) Solve the equation $\log_4(3w+1) = 2$.

3641 = (24)

Sw+1 = 16

3w = 15

W = 5 RAWW

(iii) Luka says that the equation $\log_x(4x + 12) = 2$ has only one solution.

Is he correct?

Find the solution(s), justifying your answer.

(4x412) = xc2 (tog4+logx+log12)/

(b) Make x the subject of the equation $a^{2x} = b^{x+1}$.

a22 = 62+1

a^{23c} = (3c+1) log b

i)	Assuming the exponential growth is of the form $y = A r^t$, what was the value of the house at the start of 1999 when she bought it?
	350000 = A (0.03) K
	350000
	D 11820 (0.03)
	16×3% = 48%.
	350,000 KO13
::\	A C.:
ii)	A friend also bought a house at the start of 1999 that cost \$200 000. Its market value also has been steadily increasing, but at a slightly higher exponential
	rate of 3.5%.
	Its value, \$y, t years after the start of 1999, is given by the function
	$y = 200000 \times (1.035)^t$
	If the houses continue to keep increasing in value at the original rates, in which year will the two houses be worth the same amount?
	Jet (1035)16 = 1-734
	$u = 1734 \times 200000 = 3444 \times 797$
	Worth now
	(2019)

QUESTION TWO

Simplify $\frac{2x^2 + 7x - 4}{2x^2 - 32}$ (a)

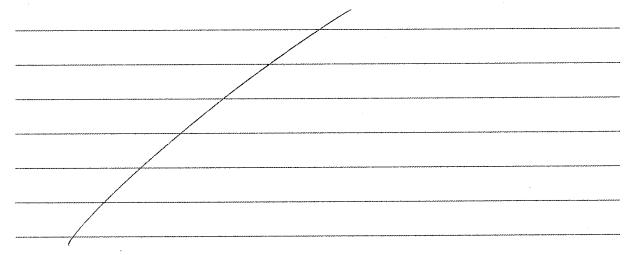
$2x^2 - 32$	(2x+1) (x/4)
	(22+8) (x-4
	· · ·

 (22+8)(x-4)	
 = 20c+1.	
2x+8	

(b) If $a = y^{\frac{3}{4}}$, find an expression for a^7 in terms of y.

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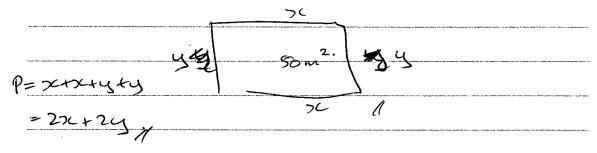
Solve the equation $2u^{\frac{2}{3}} + 7u^{\frac{1}{3}} = 4$ (c)



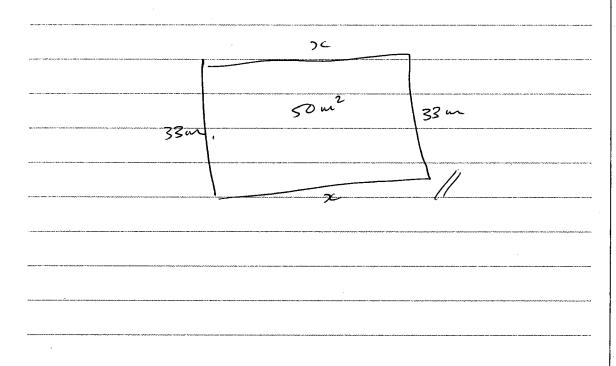
(d) Talia used timber to form the exterior sides of her rectangular garden. The length of the garden is x metres, and its area is 50 m^2 .

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(i) Show that the perimeter of the garden is given by $2x + \frac{100}{x}$



(ii) If she uses 33 m of timber to build the sides, find the dimensions of the garden.



(e)

David and Sione are competing in a cycle race of 150 km.	ASSESSOR'S USE ONLY	
Sione cycles on average 4 km per hour faster than David, and finishes half an hour earlier than David.		
Find David's average speed.		
You MUST use algebra to solve this problem. (Hint: average speed = $\frac{distance}{time}$)		
V-4km/ph = 150km		
V-4 km/ph = 150 km averagespeed, S-30		

NZ

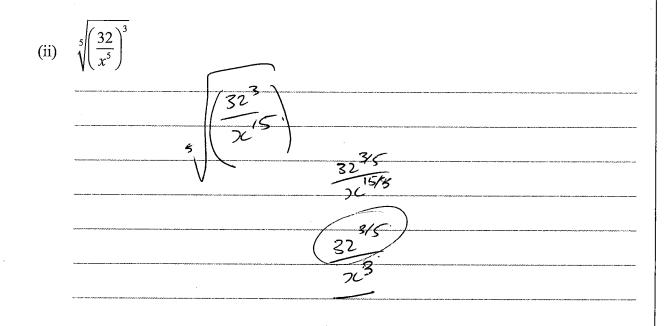
QUESTION THREE

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(a) Simplify, giving your answer with positive exponents:

(i) $\left(\frac{a^{10}}{4a^5}\right)^2$ $\left(\frac{a^{10}}{4a^5}\right)^{-2}$ $\frac{a^{-20}}{4a^{-10}} = \left(\frac{4a^{10}}{a^{20}}\right)^{-2}$	
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U,

(b) Solve the following equation for t:

$$\frac{1}{t(t-1)} - \frac{1}{t} = \frac{3}{t-1}$$

 $\frac{1}{\mathsf{t}(\mathsf{t})} - \frac{1}{\mathsf{t}} = \frac{3}{\mathsf{t}-1}$

 $\frac{1}{t(t-1)} = \frac{3}{t-1} + \frac{1}{t}$

$$\frac{1}{t^2 - t} = \frac{3}{t - 1} + \frac{1}{t}$$

t=7/

Question Three continues on the following page.

(c)

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For what value(s) of k does the graph of the quadratic function
$y = x^2 + (3k - 1)x + (2k + 10)$
never touch the x-axis? $(a=0)$ $b=(k-1)$ $c=(k+10)$
$(3k-1)^2-4\times0\times(2k+10)=0$
(3(c-1)(3(c-1)) = 0
$9k^2 - 3k - 3k - 1 = 0$
$9k^2 - 6k - 1 = 0$
K=0.539 K==0.206/

(d)	The	quadratic	equation
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$$mx^2 - (m+2)x + 2 = 0$$

has two positive real roots.

Find the possible value(s) of m, and the roots of the equation.

(- (m+2)2 -4 (m) (2 (co)
- Jm2+4m+4)-8m <0
-m²-4m-4-8m<0
-m² +12m - 4 <0
yc = 11.6C
x = 0.343.

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