## Assessment Schedule - 2022

## Physics: Demonstrate understanding of electrical systems (91526)

## Evidence

| Q | Evidence | Achievement | Merit | Excellence |
| :---: | :---: | :---: | :---: | :---: |
| ONE <br> (a) | $\begin{aligned} & X_{c}=\frac{1}{2 \pi f C}=\frac{1}{2 \pi \times 50 \times 54.0 \times 10^{-6}} \\ & =58.946 \Omega \end{aligned}$ | - Correct formula and substitution. |  |  |
| (b) | $\begin{aligned} & Z=\sqrt{R^{2}+X_{\mathrm{c}}^{2}} \\ & =\sqrt{36.0^{2}+58.9^{2}}=69.1 \Omega \\ & \text { Circuit current }=\frac{V_{\mathrm{s}}}{Z}=\frac{25.0}{69.1}=0.362 \mathrm{~A} \end{aligned}$ | - Correct answer for impedance. <br> - Correct current with incorrect impedance. | - Correct answer for circuit current. |  |
| (c) | Accept either an impedance phasor diagram or a voltage phasor diagram. <br> Current is in phase with resistor voltage: $\theta=\tan ^{-1}\left(\frac{58.9}{36.0}\right)=58.6^{\circ}$ <br> Current leads supply voltage by $58.6^{\circ}$. | - Correct phasor diagram. OR <br> Recognition that the circuit current is in phase with the resistor voltage. <br> OR <br> Correct value for phase difference <br> OR <br> States that current leads supply voltage. | - Correct value for phase difference as an angle. <br> AND <br> States that current leads supply voltage. |  |

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(d) Resonance is when the current is a maximum. Current is a maximum when impedance is minimum.
This happens when $X_{\mathrm{c}}=X_{\mathrm{L}}$ and $Z=R$ and $V_{\mathrm{s}}=$ $V_{\mathrm{R}}$.
So an inductor whose reactance is the same as that of the capacitor should be added to the circuit in order to bring this circuit to resonance.

- ONE condition for resonance.
- ONE error in answer
- Correct answer

| NØ | N1 | $\mathbf{N 2}$ | $\mathbf{A 3}$ | $\mathbf{A 4}$ | M5 | M6 | E7 | E8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No response; <br> no relevant evidence. | 1 a | 2 a | 3 a | 4 a | $1 \mathrm{a}+2 \mathrm{~m}$ | $1 \mathrm{a}+3 \mathrm{~m}$ or | $2 \mathrm{a}+1 \mathrm{~m}+1 \mathrm{e}$ | $1 \mathrm{a}+2 \mathrm{~m}+1 \mathrm{e}$ |


| Q | Evidence | Achievement | Merit | Excellence |
| :---: | :---: | :---: | :---: | :---: |
| TWO <br> (a) | $\mathrm{I}_{\max }=\frac{V_{\mathrm{s}}}{R}=\frac{12.0}{22.0}=0.545 \mathrm{~A}$ <br> Current after two time constants $=I=I_{\text {max }}\left(1-e^{-2}\right)$ $I=0.545\left(1-e^{-2}\right)=0.471 \mathrm{~A}$ | - Correct value for maximum current. <br> OR Identifies that current changes by 63\%. | - Correct answer of 0.471 A. |  |
| (b) | $V_{\mathrm{L}}=0, V_{\mathrm{R}}=12 \mathrm{~V}$ | - BOTH correct. |  |  |
| (c) | $\begin{aligned} & V=\frac{L \Delta I}{t} \\ & I=\frac{V}{R}=\frac{12.0}{22.0}=0.545 \mathrm{~A} \\ & V=\frac{1.60 \times 0.545}{2.50 \times 10^{-2}}=34.9 \mathrm{~V} \end{aligned}$ <br> Since the induced voltage opposes the change in current, it will try to prevent the current from decreasing and so will act in the same direction as the source voltage. | - Correct value of induced voltage. OR Correct direction of induced voltage | - Correct value of induced voltage. <br> AND <br> Correct direction of induced voltage |  |
| (d) | If the resistance was changed to $44.0 \Omega$, then the size of the maximum current once it was steady would halve, since $I=\frac{V}{R}$. <br> The increased resistance will have an effect on the time constant as $\tau=\frac{L}{R}$, so time constant would halve. Hence it will take less time for the current to become steady. <br> Since the energy stored in the inductor $E \mathrm{p}=\frac{1}{2} L I^{2}$, and the current has halved, the energy stored in the inductor once the current is steady would be $1 / 4$. <br> Evidence can be taken from calculations to support explanation. | - Any ONE of: <br> - current decreases <br> - time constant decreases <br> - less energy stored in the inductor. | - Any TWO statements with correct reasoning: <br> - Current decrease since $I=\frac{V}{R}$, and $R$ has doubled. <br> - Time constant decreases because R has increased. <br> Less energy is stored in the inductor as current has decreased and energy stored $=\frac{1}{2} L I^{2}$. | - Current and time constant have halved with reasons including reasoning out the energy stored in the inductor has decreased by $1 / 4$ of its original value. |


| NØ | N1 | N2 | A3 | A4 | M5 | M6 | E7 | E8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No response; no relevant evidence. | 1a | 2a | 3 a | 4a | $1 \mathrm{a}+2 \mathrm{~m}$ | $1 \mathrm{a}+3 \mathrm{~m}$ | $2 \mathrm{a}+1 \mathrm{~m}+1 \mathrm{e}$ | $1 \mathrm{a}+2 \mathrm{~m}+1 \mathrm{e}$ |


| Q | Evidence | Achievement | Merit | Excellence |
| :---: | :---: | :---: | :---: | :---: |
| THREE <br> (a) | $C=\frac{\varepsilon_{0} \varepsilon_{r} A}{d}=\frac{8.85 \times 10^{-12} \times 1.00 \times 0.16}{0.001}=1.42 \times 10^{-9} \mathrm{~F}$ | - Correct working. <br> *This is a SHOW THAT question. |  |  |
| (b) | Energy stored $\begin{aligned} & =\frac{1}{2} C V^{2}=\frac{1}{2} \times 1.42 \times 10^{-9} \times 9.00^{2} \\ & =5.75 \times 10^{-8} \mathrm{~J} \end{aligned}$ <br> Introducing a dielectric will allow more charge to be stored on the plates, thereby increasing the capacitance 7 times. <br> So, the energy stored will increase 7 times. | - Correct energy stored. <br> OR <br> Energy increases 7 times. | - Correct energy stored AND <br> Capacitance increases 7 times, so energy stored increases 7 times. |  |
| (c) | The charge on the plates remains the same. However, Capacitance, $C$, decreases as distance, $d$, between the plates increases $C=\frac{Q}{V}$. So, the voltage across the plates increases. | - One correct statement. | - Two statements with one correct reason. |  |
| (d) | Total capacitance $=\frac{1}{C_{\mathrm{T}}}=\frac{1}{470 \mu \mathrm{~F}}+\frac{1}{800 \mu \mathrm{~F}}$ $C_{\mathrm{T}}=296 \mu \mathrm{~F}$ $\text { Total charge }=Q_{\mathrm{T}}=C_{\mathrm{T}} V=296 \times 10^{-6} \times 12$ $=3.552 \times 10^{-3} \mathrm{C}$ <br> Voltage across $470 \mu \mathrm{~F}$ capacitor: $V=\frac{Q}{C}=\frac{3.552 \times 10^{-3}}{470 \times 10^{-6}}=7.56 \mathrm{~V}$ | - Total capacitance. <br> OR <br> Total charge with incorrect capacitance. | - Total charge. <br> OR <br> One error in calculation. | - Correct answer for voltage. |


| NØ | $\mathbf{N 1}$ | $\mathbf{N} \mathbf{2}$ | $\mathbf{A 3}$ | $\mathbf{A 4}$ | M5 | M6 | E7 | E8 |
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| No response; <br> no relevant evidence. | 1 a | 2 a | 3 a | 4 a | $1 \mathrm{a}+2 \mathrm{~m}$ | $1 \mathrm{a}+3 \mathrm{~m}$ | $2 \mathrm{a}+1 \mathrm{~m}+1 \mathrm{e}$ |  |

## Cut Scores

| Not Achieved | Achievement | Achievement with Merit | Achievement with Excellence |
| :---: | :---: | :---: | :---: |
| $0-7$ | $8-13$ | $14-18$ | $19-24$ |

